# An introduction to the tunedinerter-damper for vibration suppression

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#### **Presentation overview**

- The need for vibration suppression devices
- The inerter
- The tuned-inerter-damper (TID)
- Design based on TMD design rules
- Application to MDOF systems
- Experimental results
- Example of TID used to suppress cable vibration
- Summary and Acknowledgements

### Vibration suppression: bridges









## Vibration supression: tall buildings



Taipei 101, completed in 2003, 508 m high. Uses a tuned-mass-damper

#### **Vibration suppression: space structures**



International Space Station (ISS) with deployable solar arrays. Attitude control using gyros.

#### **Vibration suppression: helicopters**



Sikorsky S-76, uses a bifilar vibration absorbers (centrifugal pendulum absorber)

# **Other systems**







#### The inerter

The inerter was introduced by Malcolm Smith (Cambridge), to complete the force-current analogy between mechanical and electrical networks.

Mechanical Networks		Electrical Networks	
Spring F=k(x <sub>2</sub> -x <sub>1</sub> )	k K X1 F X2	Inductor $F=1/L(x_2-x_1)$	1/L
Damper $F=c(\dot{x}_2-\dot{x}_1)$	$ \begin{array}{c}                                     $	<b>Resistor</b> $F=1/R(\dot{x}_2-\dot{x}_1)$	$1/R$ $1/R$ $1/X_1$ $1/X_2$
Inerter $F=b(\ddot{x_2}-\ddot{x_1})$	$F$ $X_1$ $X_2$	Capacitor F=C(x2-x1)	$C$ $X_1$ $i \swarrow X_2$

## **Types of inerter**

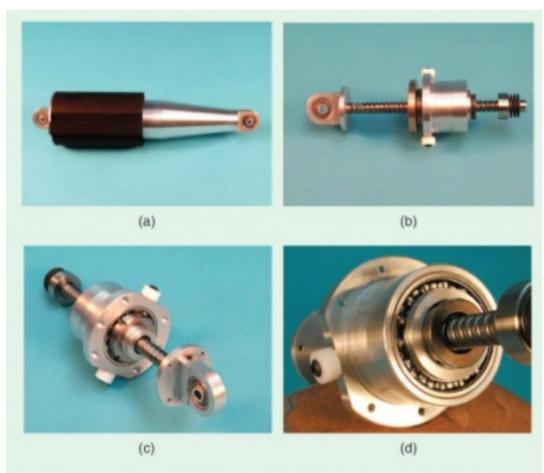
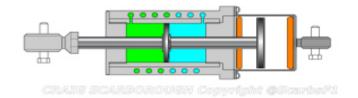
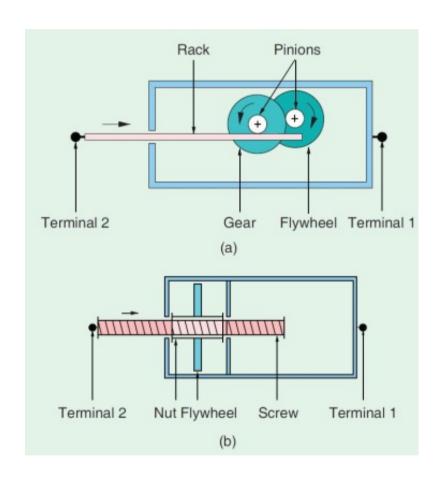


Figure 4. Ballscrew inerter made at Cambridge University Engineering Department; Mass ≈1 kg, Inertance (adjustable) = 60-240 kg. (a) Complete with outer case, (b) ballscrew, nut and flywheel, (c) flywheel removed, (d) thrust bearing.

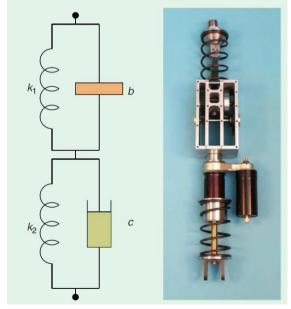


Proposed new 'Fluid Inerter'

#### The inerter in Formula 1 suspensions



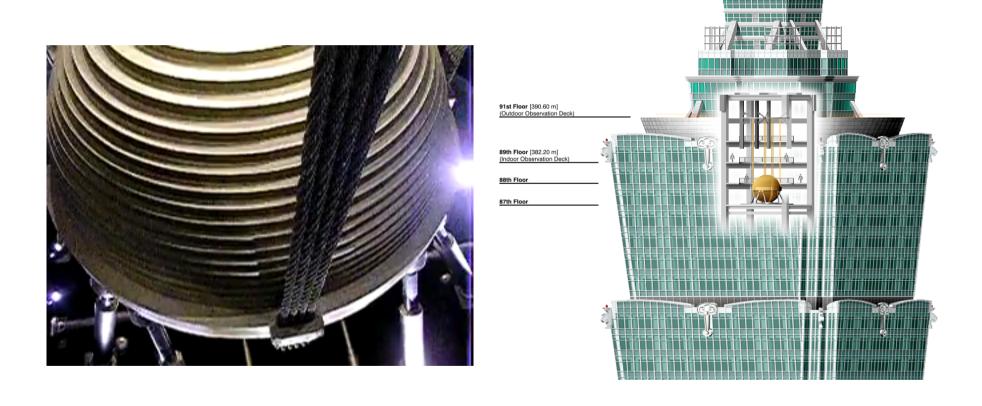




First used by McLaren Mercedes as the "J-damper" in 2005. Inerter unit is tuned to the tire natural frequency to maintain maximum tire contact patch area.

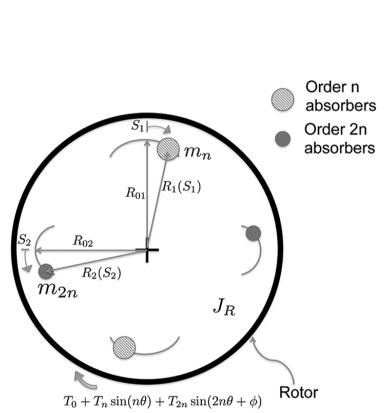
#### The inerter in structural control

The F1 concept has some similarities to a tuned mass damper (TMD)



Taipei 101 tuned mass damper 660-tonne mass

#### Bifilar vibration absorber

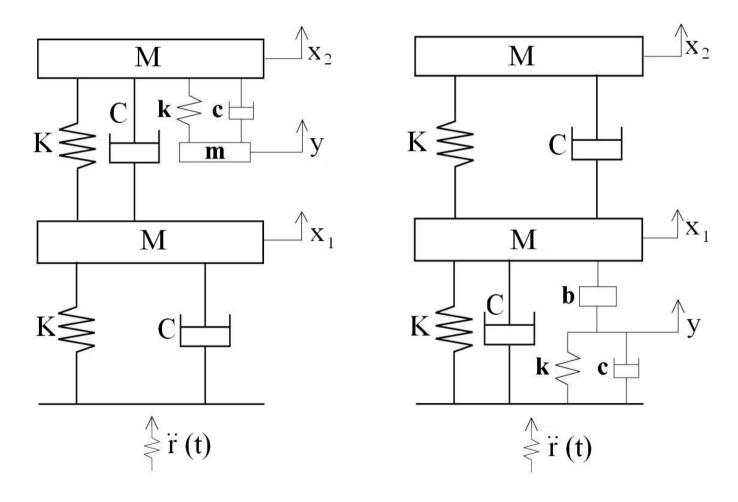




Shaw et. al J. Vib. Acoust. 135(6), 061012 (Aug 06, 2013)

## The tuned-inerter-damper (TID)

A tuned-inerter-damper (TID) can be developed using a similar ethos to that described by Den Hartog for the TMD.



## **Design and tuning a TID**

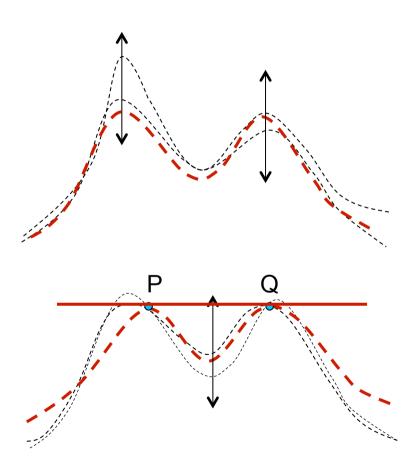
For base excitation, the following steps are required:

Step 1 Specify inertence to mass ratio:

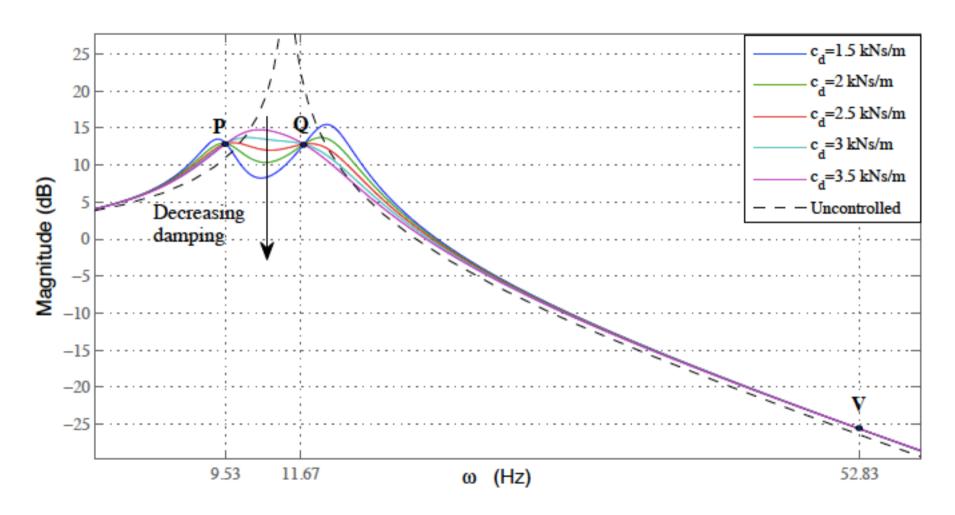
$$b = \mu_b M$$

Step 2 Calibrate  $k_{d_{TID}}$  such that the 2 peaks have almost equal ordinates. The TMD tuning rule given by Den Hartog was used as an initial guess.

Step 3 Calibrate  $C_{d_{\mbox{\scriptsize TID}}}$  such that one of the 2 peaks has a horizontal tangent in one of the two common points



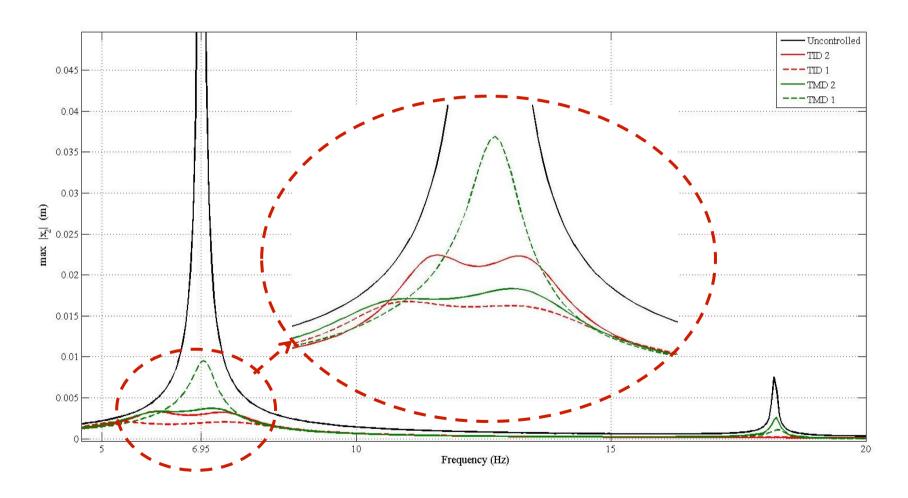
## **TID tuning example**



For base excitation, there are 3 fixed points instead of 2 (as for TMD). The related cubic equation is solved numerically.

## **Comparison of TID and TMD**

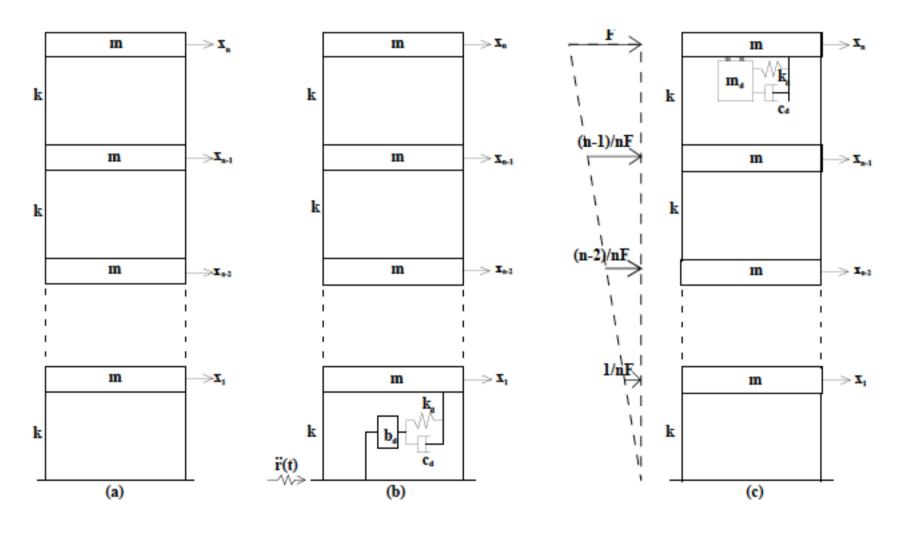
The TID can generate a high inertia force with a relatively low mass.



Notice that the TID reduces the amplitude around the second mode

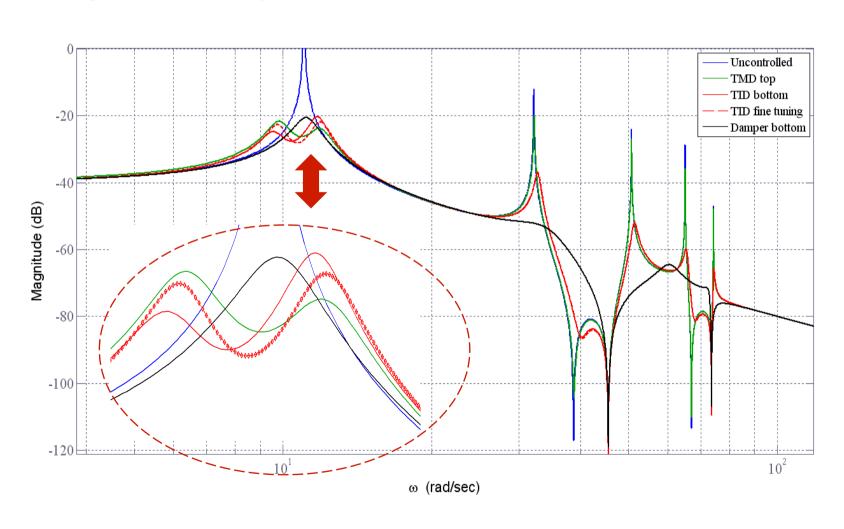
## More degrees-of-freedom

The concept can be extended to more degrees-of-freedom



## More degrees-of-freedom

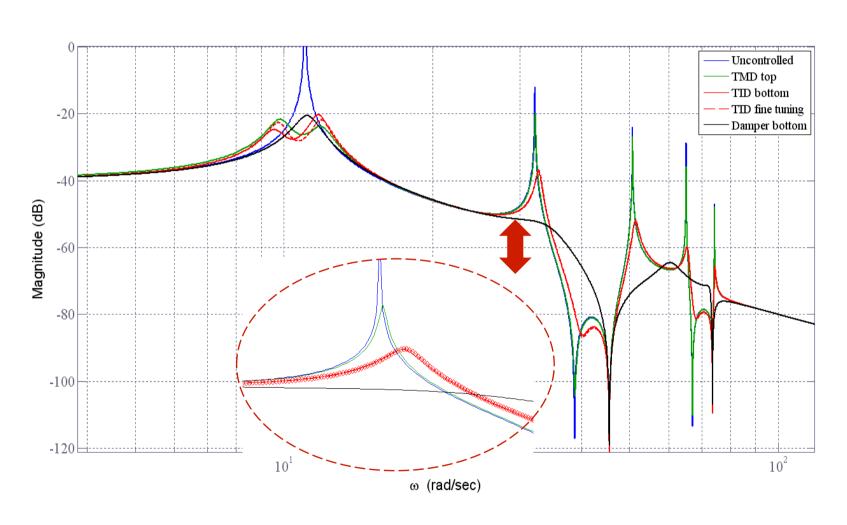
A five degree-of-freedom system with sinusoidal base excitation.



The damper curve is for a damper constant that is 12 times larger than the TID damper

## **Effect on higher modes**

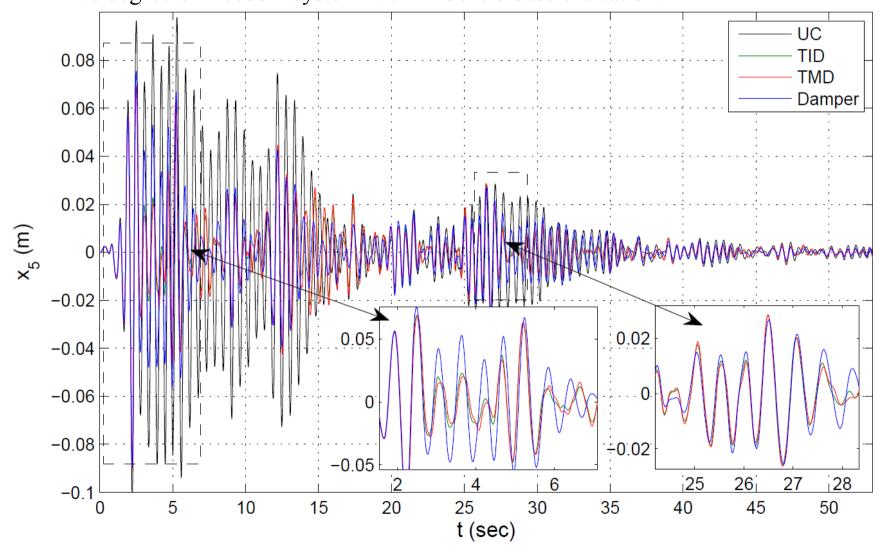
A five degree-of-freedom system with sinusoidal base excitation.



The TID reduces the amplitude in the higher modes

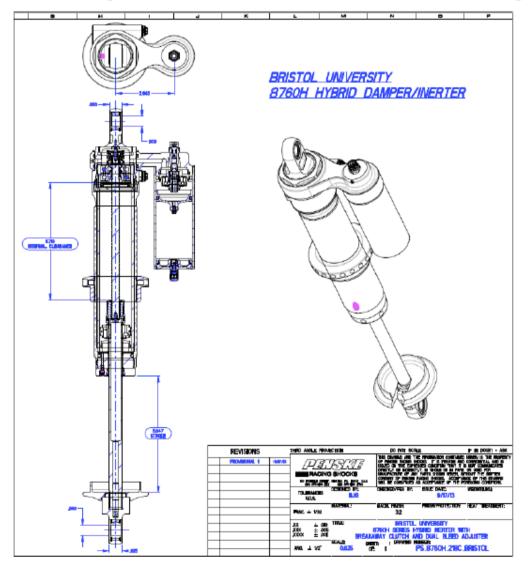
## **TID: Earthquake excitation**

A five degree-of-freedom system with El Centro base excitation.



#### **Commercial inerter from Penske**

2.25kg mass and the maximum inertance is 75kg

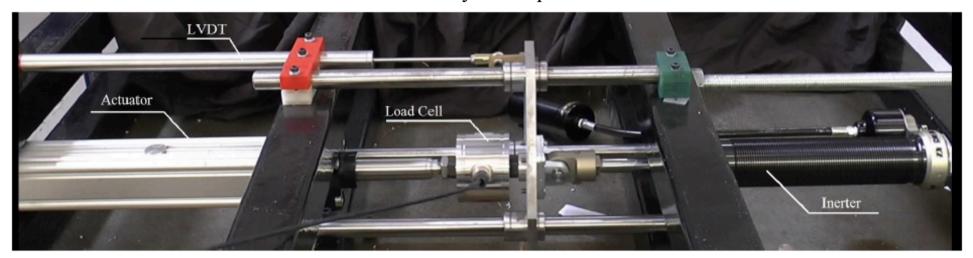


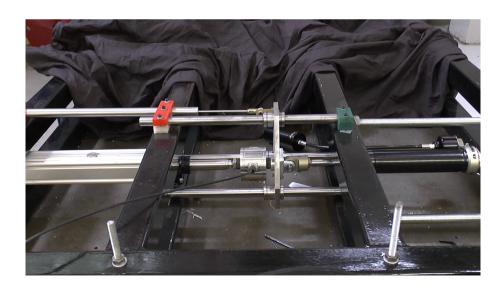


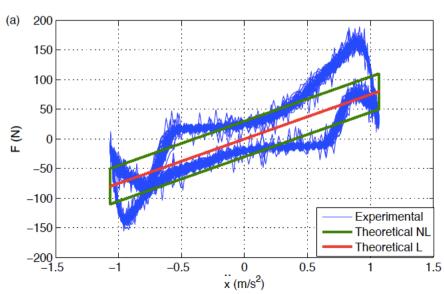
The maximum stroke is 140mm, dry friction damping approx 30Ns/m

## **TID:** hybrid tests

The Penske inerter was used in a series of hybrid experimental tests to simulate a TID

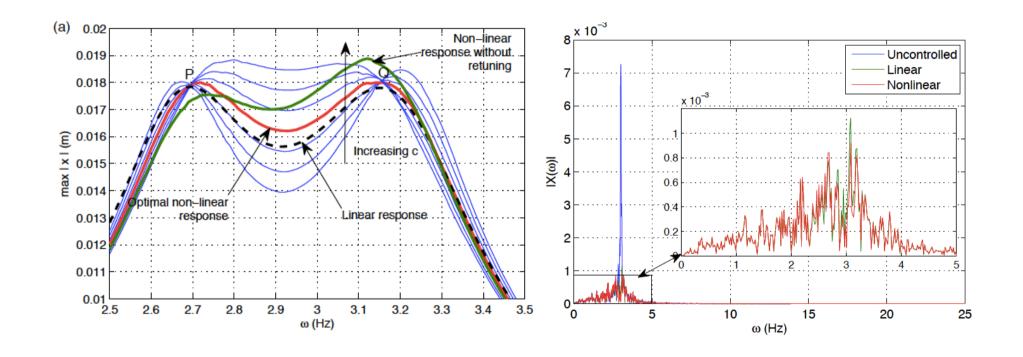




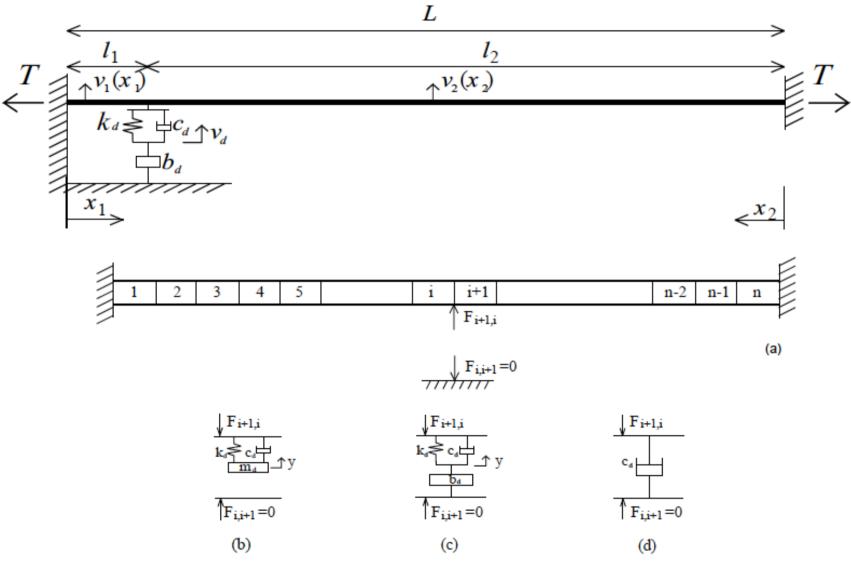


#### **TID: validated nonlinear model**

The experimental results were used to validate the numerical model.



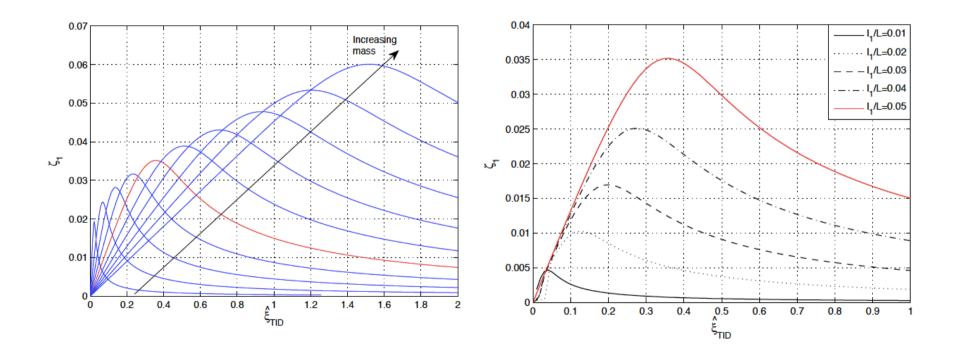
## **TID:** applied to cable vibration



Finite element model used to discretize the cable

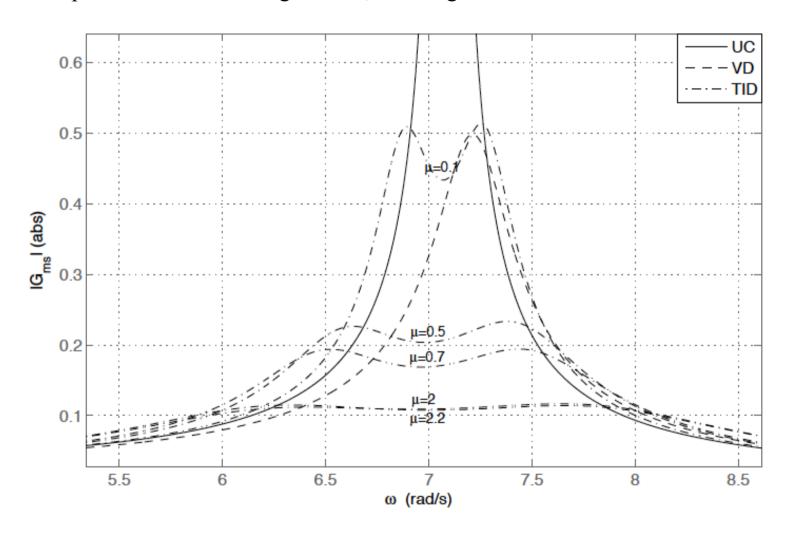
#### **TID:** cable results

Increasing mass (inertance) or distance ratio, increases modal damping in cable up to a maxium, and then decreases the value



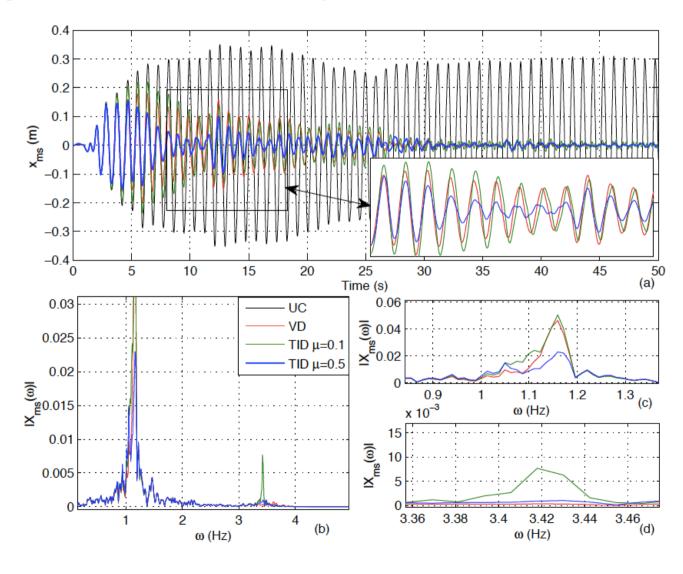
#### **TID:** cable results

Bode plots for TID on a single cable, showing mode 1 resonance



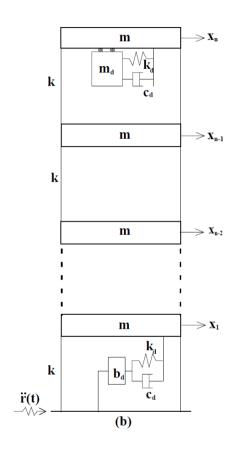
#### **TID:** cable results

Earthquake excitation for TID on a single cable



#### **TID: Summary**

- The TID is a new concept (Tuned Viscous Mass Damper, TVMD 2011)
- A TID can be designed using simple rules like a TMD
- A TID is optimum at the base of the structure
- The TID can produce high inertial forces with a lower overall mass
   application for lightweight structures
- The TID can damp amplitudes of higher modes
- It is at an early stage of experimental testing and development



#### Papers:

#### **EACS 2016 in Sheffield**



Faculty of Engineering has 7 Departments: 260 Academic staff; 3300 Undergraduate students 700 Research students; 700 Postgraduate taught students 11<sup>th</sup> to 13<sup>th</sup> July 2016

Abstract deadline: 15th Jan 2016

http://eacs2016.co.uk

RASD ISVR is week before





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#### Where is Sheffield?





## **Acknowledgements**





Irina Lazar



Simon Neild



Alicia Gonzalez-Buelga

## Thank you for your attention

